

Selection rules

1) Electric dipole transition $\rightarrow \sigma$

$$H_{nn} = |\langle \psi_m | \vec{x} | \psi_n \rangle|^2$$

if $H_{nn} \neq 0$ transition occurs

$\Delta m = 0$ is forbidden

$$\Delta E$$

$$T = \frac{g}{\Delta E} \cdot \frac{g}{|\langle \psi_1 | \psi_2 \rangle|^2}$$

a) $[L_z, z] = 0 \quad (n \in m)$

$$\langle n' e' m' | L_z \cdot z - z L_z | n e m \rangle =$$

$$= \hbar (m' - m) \langle n' e' m' | z | n e m \rangle = 0$$

$m' - m = 0$ for polarized in σ direction

σ - transition

b) $[L_z, x \pm iy] = \pm \hbar (x \pm iy)$

$$\langle n' e' m' | (z(x \pm iy) - (x \pm iy)L_z) | n e m \rangle =$$

$$= \hbar (m' - m) \langle n' e' m' | x \pm iy | n e m \rangle$$

$$= \pm \hbar \langle n' e' m' | x \pm iy | n e m \rangle$$

$\Rightarrow m' - m = \pm 1$ for light polarized transverse to z

σ - transition

$$\Leftrightarrow [L^2, [L^2, \times]] = 2\lambda^2 (x L^2 + L^2 x)$$

$$(\ell + \ell')(\ell + \ell' + 2)[(\ell - \ell')^2 - 1] \langle n \ell m | x | n' \ell' m' \rangle = 0$$

$$\ell, \ell' > 0$$

$$\ell - \ell' = \pm 1$$

Wigner - Eckart Theorem //

2) magnetic dipole transition

$$\langle n \ell m | \mu | n' \ell' m' \rangle$$

on L - even parity

the states have the same parity

1) & 2)

21cm line \rightarrow lifetime 10 millions years